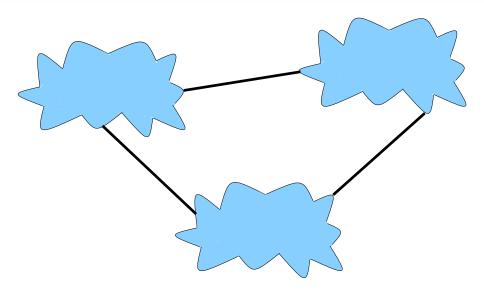
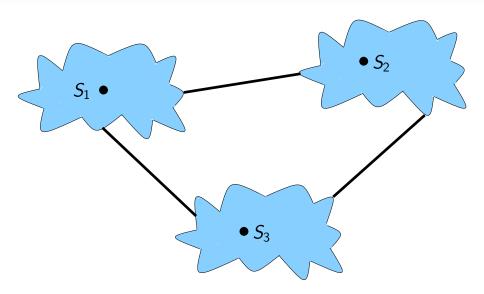
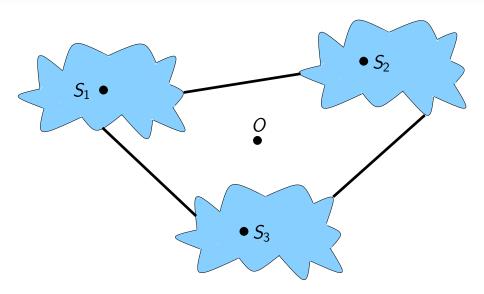
# Monotony in Service Orchestrations

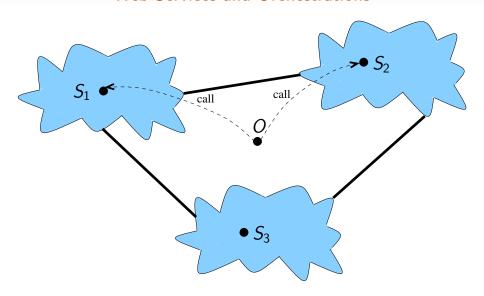
A. Bouillard S. Rosario A. Benveniste S. Haar

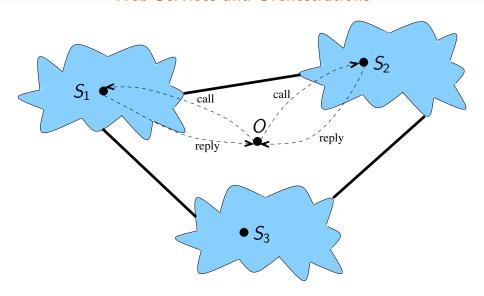
May 20, 2008

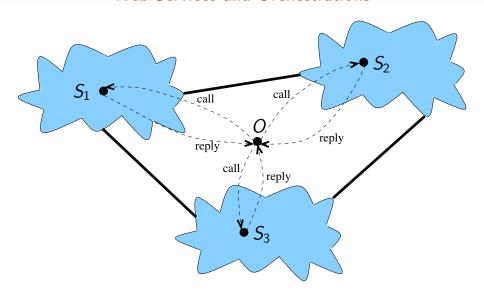




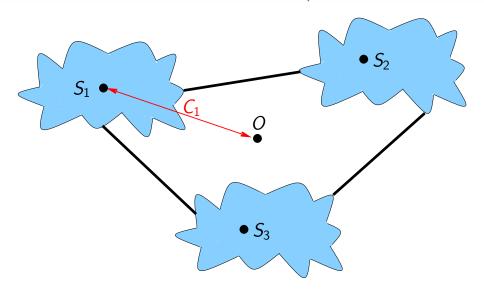




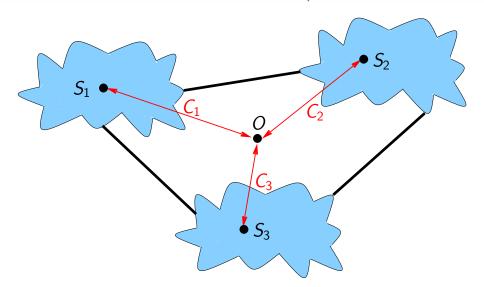


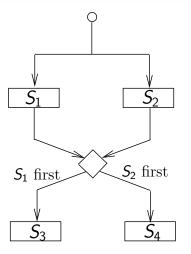


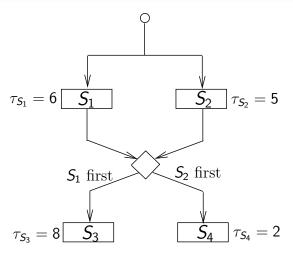
# Contract, Contract Composition

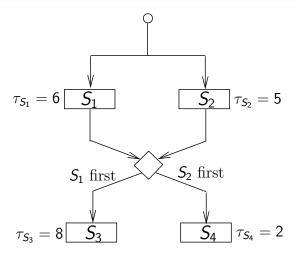


# Contract, Contract Composition

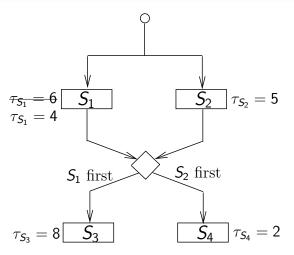


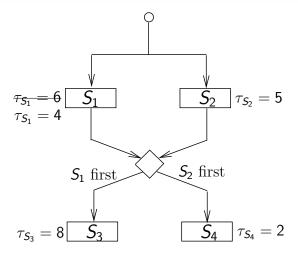




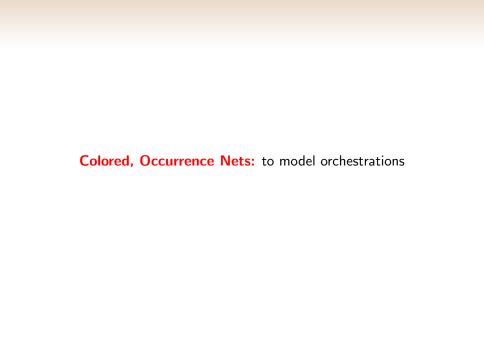


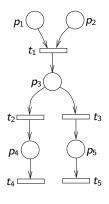
Overall latency :  $\tau_{S_2} + \tau_{S_4} = 7$ 





Overall latency :  $\tau_{S_1} + \tau_{S_3} = 12$ 





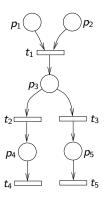
$$N=(\mathcal{P},\mathcal{T},\mathcal{F},M_0)$$

 $\ensuremath{\mathcal{P}}$  : Set of Places

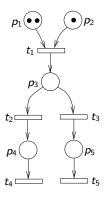
 $\ensuremath{\mathcal{T}}$  : Set of Transitions

 $\mathcal{F}\subseteq (\mathcal{P}\times\mathcal{T})\cup (\mathcal{T}\times\mathcal{P})$  : Flow Relation

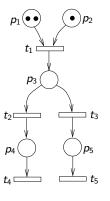
 $M_0:\mathcal{P} \to \mathbb{N}$ : Initial Marking



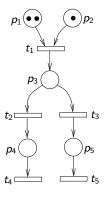
$$\begin{aligned} \textit{M}_0 &= \{\textit{p}_1 \to 2, \textit{p}_2 \to 1, \textit{p}_3 \to 0 \\ \textit{p}_4 &\to 0, \textit{p}_5 \to 0 \} \end{aligned}$$



$$M_0 = \{ p_1 \to 2, p_2 \to 1, p_3 \to 0 \\ p_4 \to 0, p_5 \to 0 \}$$

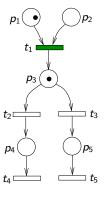


**Preset** of a node x:  ${}^{\bullet}x$  for e.g,  ${}^{\bullet}t_1 = \{p_1, p_2\}$ 

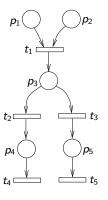


**Preset** of a node x:  $^{\bullet}x$  for e.g,  $^{\bullet}t_1 = \{p_1, p_2\}$ 

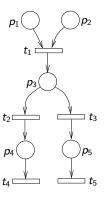
Postset of a node  $x: x^{\bullet}$  for  $e.g, t_1^{\bullet} = \{p_3\}$ 



Firing of transition  $t_1$ 



Causality Relation :  $\leq$  for e.g, :  $ho_3 < t_1 < 
ho_1$   $t_1 < t_2 < t_4$ 



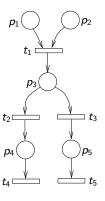
**Causality** Relation : ≤

for e.g, :  $\emph{p}_3 < \emph{t}_1 < \emph{p}_1$ 

 $t_1 < t_2 < t_4$ 

Conflict Relation: #

for e.g, :  $t_2 \# t_3$ 



Causality Relation :  $\leq$ 

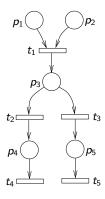
for e.g, :  $p_3 < t_1 < p_1$ 

 $t_1 < t_2 < t_4$ 

Conflict Relation: #

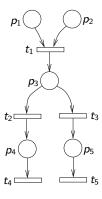
for e.g, :  $t_2\#t_3$ 

 $t_4 \# t_5$ 



#### A **configuration** is a sub-net $\kappa$ s.t.:

1.  $\kappa$  is causally closed. If  $x \in \kappa$  and x' < x, then  $x' \in \kappa$ .



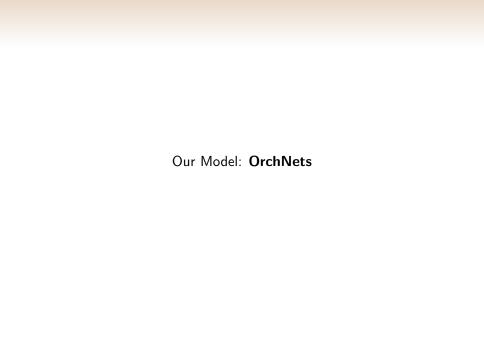
#### A **configuration** is a sub-net $\kappa$ s.t.:

- 1.  $\kappa$  is causally closed. If  $x \in \kappa$  and x' < x, then  $x' \in \kappa$ .
- 2.  $\kappa$  is conflict-free.  $\nexists x, x' \in \kappa \ s.t. \ x \# x'$

#### Occurrence Nets

A safe net N is called an occurrence net iff

- 1. No node of *N* is in self-conflict.
- $2. \le is a partial order$
- 3.  $\lceil t \rceil = \{x \in N \mid x \le t\}$  is finite for all transitions of N.
- 4.  $| \cdot p | \le 1$  for all places of N.



# **OrchNets**

• Tokens have *colors*: (value, date)

#### **OrchNets**

- Tokens have colors: (value, date)
- A transition t has functions  $(\phi_t, \tau_t)$  that modify the token colors.

An *OrchNet* is a tuple  $\mathcal{N} = (N, \Phi, T, T_{\text{init}})$ 

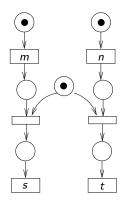
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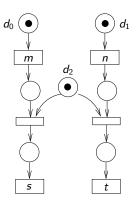
- N: occurrence net with token attributes c = (value, date).
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- $\Phi = (\phi_t)_{t \in \mathcal{T}}$ : family of value functions.
- $T = (\tau_t)_{t \in \mathcal{T}}$ : family of *latency functions*.
- $T_{\text{init}} = (\tau_p)_{p \in \min(\mathcal{P})}$ : family of *initial date functions*.

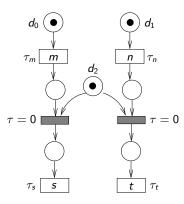
# OrchNets: Example

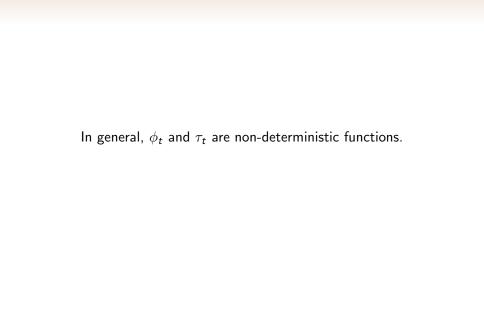


# OrchNets: Example



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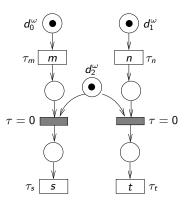


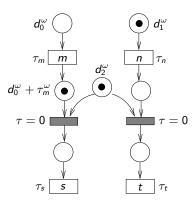


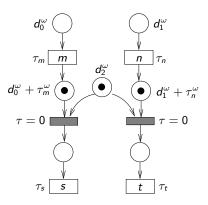
 $\omega \in \Omega$ , a **daemon** variable that resolves non-determinism.

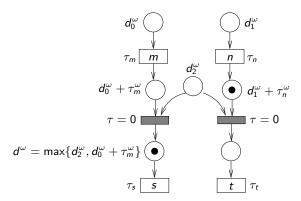
 $\omega \in \Omega$ , a **daemon** variable that resolves non-determinism.

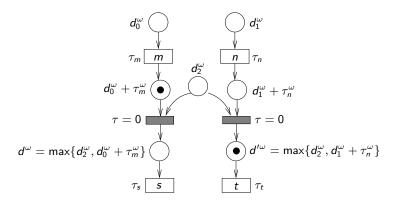
For a given value of  $\omega$ ,  $\phi_t^\omega$  and  $\tau_t^\omega$  are deterministic functions.

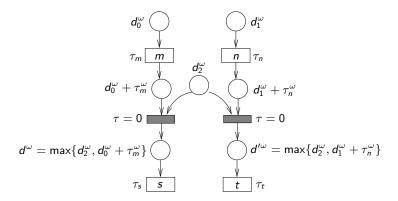








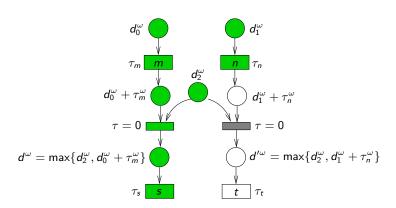




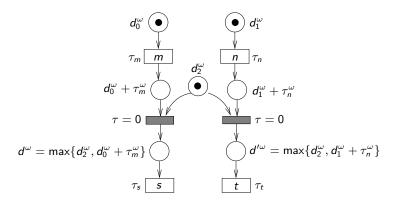
Actually occurring configuration for a given  $\omega$ :  $\overline{\kappa}(\mathcal{N}, \omega)$ 

When  $d^{\omega} < d'^{\omega}$ ,  $\overline{\kappa}(\mathcal{N}, \omega)$  is..

# When $d^{\omega} < d'^{\omega}$ , $\overline{\kappa}(\mathcal{N}, \omega)$ is..



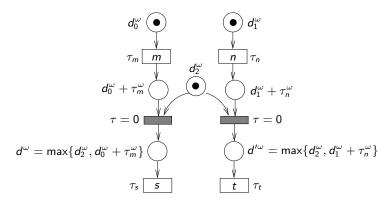
#### **Execution Time**



**Execution Time** of a maximal configuration  $\overline{\kappa}$  of  $\mathcal{N}$ :

$$E_{\omega}(\overline{\kappa}, \mathcal{N}) = \{ max(d_{x}^{\omega}) \mid x \in \overline{\kappa} \}$$

#### **Execution Time**

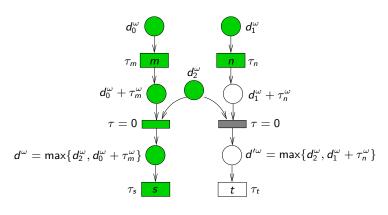


For a given  $\omega$ , execution time of  $\mathcal{N}$ :

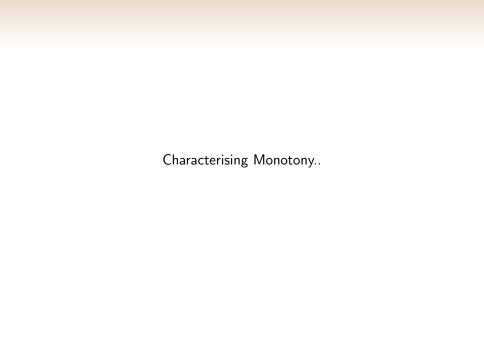
$$E_{\omega}(\mathcal{N}) = E_{\omega}(\overline{\kappa}(\mathcal{N}, \omega), \mathcal{N})$$

# When $d^{\omega} < d'^{\omega}$ ..

#### When $d^{\omega} < d'^{\omega}$ ...



$$E_{\omega}(\mathcal{N}) = d^{\omega} + \tau_{s}^{\omega}$$



Call pre-OrchNet a tuple  $\mathbb{N} = (\textit{N}, \Phi, \mathbb{T}, \mathbb{T}_{\mathrm{init}})$  where,

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- 3.  $\mathbb{T}_{\mathrm{init}}$ : sets of families of initial date functions  $T_{\mathrm{init}}$ .

Write  $\mathcal{N} \in \mathbb{N}$  if there exists  $T \in \mathbb{T}$  and  $T_{\mathrm{init}} \in \mathbb{T}_{\mathrm{init}}$  s.t.

$$\mathcal{N} = (N, \Phi, \textit{T}, \textit{T}_{\rm init})$$

#### Pre-Orchnets: Order Relation

For two families T and T' of latency functions, write

$$T \geq T'$$

$$\text{if } \forall \omega \in \Omega, \forall t \in \mathcal{T} \implies \tau_t^\omega \geq \tau_t^{'\omega}.$$

#### Pre-Orchnets: Order Relation

For two families T and  $T^{\prime}$  of latency functions, write

$$\text{if }\forall\omega\in\Omega,\forall t\in\mathcal{T}\implies\tau_t^\omega\geq\tau_t^{'\omega}.$$

For  $\mathcal{N}, \mathcal{N}' \in \mathbb{N}$ , write

$$\mathcal{N} \geq \mathcal{N}'$$

if  $T \geq T'$  and  $T_{\rm init} \geq T'_{\rm init}$  both hold.

# Monotony: Definition

### Monotony: Definition

Pre-Orchnet  $\mathbb{N} = (N, \Phi, \mathbb{T}, \mathbb{T}_{\mathrm{init}})$  is called **monotonic** if,  $\forall \mathcal{N}, \mathcal{N}' \in \mathbb{N}$  s.t.  $\mathcal{N} \geq \mathcal{N}'$ ,

$$E_{\omega}(\mathcal{N}) \geq E_{\omega}(\mathcal{N}')$$

holds.

Pre-Orchnet  $\mathbb{N} = (N, \Phi, \mathbb{T}, \mathbb{T}_{\mathrm{init}})$  is monotonic if:

$$\forall \mathcal{N} \in \mathbb{N}, \quad \forall \omega \in \Omega, \ \forall \overline{\kappa} \in \overline{\mathcal{V}}(N),$$

$$E_{\omega}(\overline{\kappa}, \mathcal{N}) \geq E_{\omega}(\overline{\kappa}(\mathcal{N}, \omega), \mathcal{N})$$

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$$E_{\omega}(\overline{\kappa},\mathcal{N}) \geq E_{\omega}(\overline{\kappa}(\mathcal{N},\omega),\mathcal{N})$$

where  $\overline{\mathcal{V}}(N)$  is the set of all maximal configurations of N.

Proof: Let  $\mathcal{N}' \geq \mathcal{N}$ , then

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*Proof:* Let 
$$\mathcal{N}' \geq \mathcal{N}$$
, then

$$E_{\omega}(\mathcal{N}') = E_{\omega}(\overline{\kappa}(\mathcal{N}',\omega),\mathcal{N}')$$

Pre-Orchnet  $\mathbb{N} = (N, \Phi, \mathbb{T}, \mathbb{T}_{init})$  is monotonic if:

$$orall \mathcal{N} \in \mathbb{N}, \quad orall \omega \in \Omega, \ orall \overline{\kappa} \in \overline{\mathcal{V}}\left(\mathcal{N}\right),$$

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Proof: Let 
$$\mathcal{N}' \geq \mathcal{N}$$
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$$E_{\omega}(\mathcal{N}') = E_{\omega}(\overline{\kappa}(\mathcal{N}', \omega), \mathcal{N}') \geq E_{\omega}(\overline{\kappa}(\mathcal{N}', \omega), \mathcal{N})$$
  
$$\geq E_{\omega}(\overline{\kappa}(\mathcal{N}, \omega), \mathcal{N}) = E_{\omega}(\mathcal{N})$$

# A Necessary Condition ..

### A Necessary Condition ..

If the sufficient condition

$$orall \mathcal{N} \in \mathbb{N}, \quad \forall \omega \in \Omega, \forall \overline{\kappa} \in \overline{\mathcal{V}}(N),$$

$$E_{\omega}(\overline{\kappa}, \mathcal{N}) \geq E_{\omega}(\overline{\kappa}(\mathcal{N}, \omega), \mathcal{N})$$

is violated,

### A Necessary Condition ..

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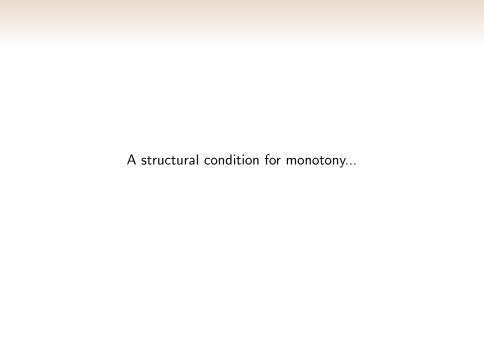
$$orall \mathcal{N} \in \mathbb{N}, \quad orall \omega \in \Omega, orall \overline{\kappa} \in \overline{\mathcal{V}}(N),$$

$$E_{\omega}(\overline{\kappa}, \mathcal{N}) > E_{\omega}(\overline{\kappa}(\mathcal{N}, \omega), \mathcal{N})$$

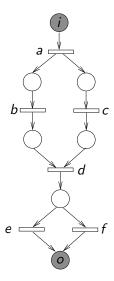
is violated, and for any two OrchNets  $\mathcal{N}, \mathcal{N}'$  s.t  $\mathcal{N} \in \mathbb{N}$ ,

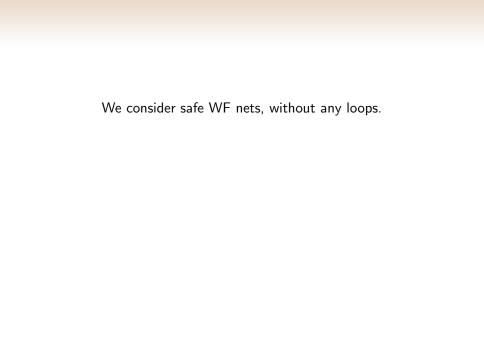
$$\mathcal{N}' \geq \mathcal{N} \implies \mathcal{N}' \in \mathbb{N}$$

holds, then  $\mathbb{N}$  is not monotonic.



# Workflow nets (WFnets)





We consider safe WF nets, without any loops.

(W,

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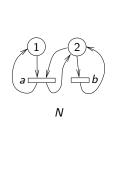
$$(W, \Phi, \mathbb{T}, \mathbb{T}_{init})$$
: pre-WFnet

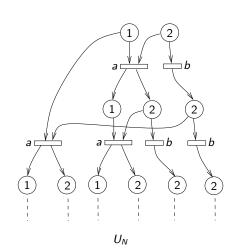
We consider safe WF nets, without any loops.

$$(W, \Phi, \mathbb{T}, \mathbb{T}_{\mathrm{init}})$$
: pre-WFnet

Unfolding W gives the occurrence net  $N_W$  and a corresponding Orchnet

$$(N_W, \Phi_W, \mathbb{T}_W, \mathbb{T}_{init})$$



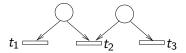


#### Clusters.

For a safe net N, a *cluster* is a minimal set  $\mathbf{c}$  of places and transitions of N such that

$$\forall t \in \mathbf{c} \implies {}^{\bullet}t \subseteq \mathbf{c} \quad , \quad \forall p \in \mathbf{c} \implies p^{\bullet} \subseteq \mathbf{c}$$

### Clusters



 $t_1,\,t_2,\,t_3$  are in the same cluster

# Sufficient Condition for Monotony of WFnets

W: WFnet,  $N_W$ : unfolding of W.

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W: WFnet,  $N_W$ : unfolding of W.

Pre-Orchnet  $\mathbb{N}_W = (N_W, \Phi_W, \mathbb{T}_W, \mathbb{T}_{\mathrm{init}})$  is monotonic if every cluster c of W satisfies:

$$\forall t_1, t_2 \in c, \ t_1 \neq t_2 \implies t_1^{\bullet} = t_2^{\bullet}$$

0	nly a very restricted class of nets are indeed monotonic.

### Conditional Monotony..

Conditional Monotony: Compare execution times only for identical responses.

#### In Conclusion...

- Identified and defined the problem of monotony in service compositions.
- Insights and reconsideration into the formulation of contracts.

#### Future Work...

• Extend the notion of monotony to probabilistic contracts.

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- Extend the notion of monotony to probabilistic contracts.
- Consider more, QoS parameters in our study.

