

# Formal Methods

## LaBRI

- Computational linguistics.
- Logic, graphs and languages.
- Modelling and Verification.

**Project SIGNES:** Common project of LaBRI, INRIA Futur and Language department of Bordeaux III.

## FRENCH SIGN LANGUAGE

- Accumulating and annotating the examples.
- Grammatical analysis of the language. Formalisation in generative grammars.

## GENERATIVE GRAMMARS

- A tighter integration of morphology and syntax. Automatic computation of semantic representations from syntactic analyses.
- Generative grammars for language fragments.

## GRAIL

- Tool for the development and prototyping of grammar fragments for categorical logics.
- Annotated dictionary of Dutch language.

## OBJECTS OF STUDY

- Models of: computer systems, data structures, semantic representations.
  - Words, trees, graphs, hyper-graphs.
- Formalisms to talk about their properties.
  - First-order logic, monadic second-order logic, the mu-calculus
- Verification, synthesis, evaluation of queries.
  - Automata, equation systems, algebra, games.

## LGL: CONT (1)

### DECOMPOSITION AND STRUCTURING OF GRAPHS (COURCELLE)

- Combinatorial structure: tree-width, clique-width,...
- Algebraic decompositions: vertex replacement, hyperedge replacement.
- Research directions:
  - Better understanding of the theory (Proof of Seese conjecture)
  - Application to query evaluation, routing, representation of maps.

### EXTERNAL DEFINITIONS (SENIZERGUES, WALUKIEWICZ)

- Rewriting systems.
- Graphs of configurations of machines (eg. pushdown automata).
- Extensions to higher-order stacks, recursive program schemes.
- Verification problems for such graphs.

## LGL CONT. (2)

### NON-REGULAR LANGUAGES (SENIZERGUES, WEIL)

- Decidability of language equivalence of deterministic pushdown automata (DPDA). Extension to decidability of bisimilarity.
- Automata of iterated stacks.
- Computation in standard algebraic structures: monoids, groups.
- Traces: words with concurrency information.

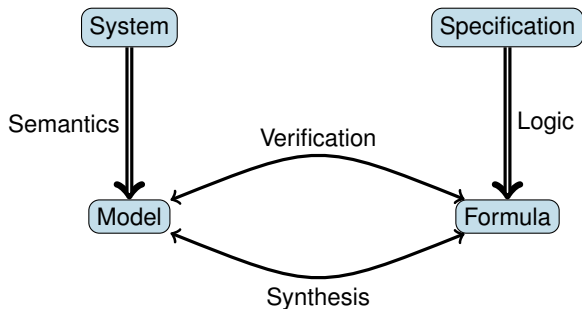
### VISUALIZATION AND SIMULATION OF DISTRIBUTED ALGORITHMS (MOSBAH)

- Simulation and visualization environment for distributed algorithms.
- On the crossroads of distributed algorithms, graph theory and rewriting systems.

### COQ: PROOF ASSISTANT (CASTERAN)

- Formalisation of induction principles (ordinals)
- Verification of a Java-card.
- The first book on Coq: Y. Bertot and P. Casteran.

# MODELLING AND VERIFICATION



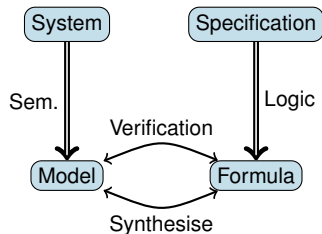
## VERIFICATION (MODEL CHECKING) [ARNOLD, CLARKE, EMERSON, SIFAKIS]

Given a model  $M$  and formula  $\alpha$  check if  $M$  satisfies  $\alpha$ .

## SYNTHESIS

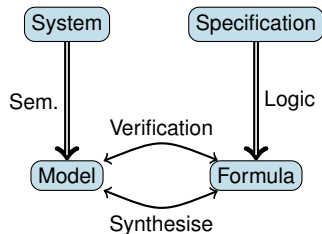
Given a formula  $\alpha$ , find a model  $M$  that satisfies  $\alpha$ .

## MV: THEORY (JANIN, MUSCHOLL, WALUKIEWICZ, ZEITUN)



- Formalisms for verification.
- Game theory
- Verification of recursive programs.
- Verification of concurrent systems.
- Synthesis.

## MV: THEORY (JANIN, MUSCHOLL, WALUKIEWICZ, ZEITUN)

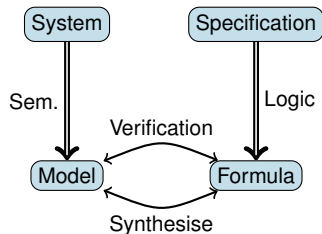


- Formalisms for verification.
  - Expressive power.
  - Algorithmic properties (model checking, satisfiability)
- Game theory
- Verification of recursive programs.
- Verification of concurrent systems.
- Synthesis.

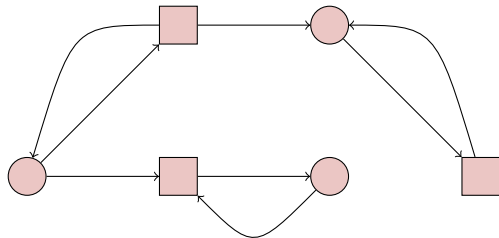
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- First-order logic,
  - monadic second order logic,
  - modal logics, the mu-calculus,
  - temporal logics, LTL, CTL



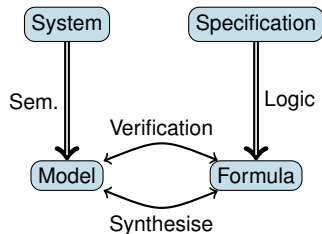
## MV: THEORY (JANIN, MUSCHOLL, WALUKIEWICZ, ZEITUN)



- Formalisms for verification.
- **Game theory**
  - Solving games.
  - Quality of strategies.
- Verification of recursive programs.
- Verification of concurrent systems.
- Synthesis.



Infinite duration two player games. Winning conditions of type: Büchi, Muller,...



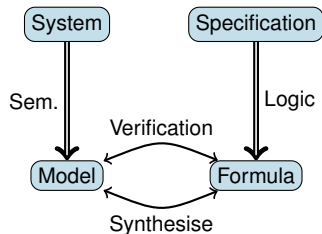
- Formalisms for verification.
- Game theory
- Verification of recursive programs.
  - Theory of stack automata and recursive schemes
  - Program semantics.
- Verification of concurrent systems.
- Synthesis.

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```
Fib(n+2) := Fib(n)+Fib(n+1);
```

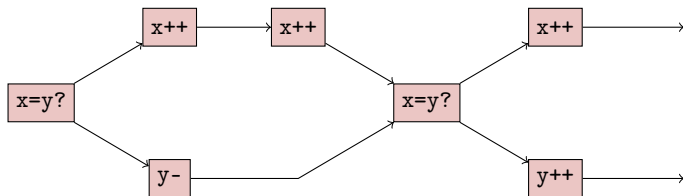
```
map(f,list)=cons(  
    f(head(list)),  
    map(f,tail(list))  
);
```

# MV: THEORY (JANIN, MUSCHOLL, WALUKIEWICZ, ZEITUN)

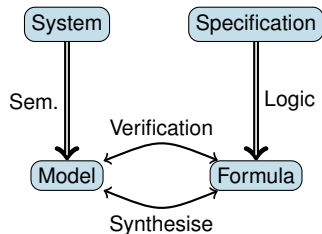


- Formalisms for verification.
- Game theory
- Verification of recursive programs.
- **Verification of concurrent systems.**
  - Trace theory, logics for traces.
  - Unfolding
- Synthesis.

$P_1 || P_2 || \dots || P_n$



## MV: THEORY (JANIN, MUSCHOLL, WALUKIEWICZ, ZEITUN)



- Formalisms for verification.
- Game theory
- Verification of recursive programs.
- Verification of concurrent systems.
- **Synthesis.**
  - Flexible and simple frameworks.
  - Algorithmic analysis.

$$P_1 || ?_1 || \dots || ?_k \models \alpha$$

# MV: MODELLING

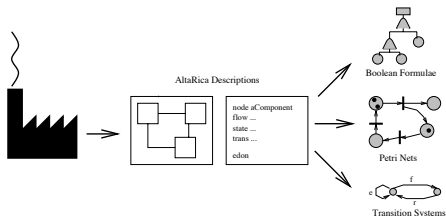
## VERIFICATION OF SYSTEMS

- Need for formal and flexible description language.
- Often limited to decidable formalisms (finite automata).
- Need for the industrial strength tools.

## VERIFICATION OF PROGRAMS

- Undecidability  $\rightarrow$  abstraction and/or/ semi-algorithms.
- Need for tools for validating and comparing different approaches.

# ALTA RICA (GRIFFAULT)



## DESIGN PRINCIPLES

- Language adapted to modelling (hierarchical, all types of communication).
- Clear mathematical semantics (finite automata).

## PARTNERS

- ONERA, IML.
- Dassault, Thales, Total, Schneider, Renault, IPSN, CEA, CFI.

# ALTA RICA CONT.

## APPLICATIONS TO SAFETY

- Fault trees.
- Minimal cuts.
- Stochastic Petri Nets.
- Scenarios.

## INDUSTRIAL IMPLEMENTATIONS

- AltaRica DataFlow.
- OCAS (Dassault).
- Combava (ARboost).
- SIMFIA V2 (EADS).

## A COMMUNITY

- Common formalism. A large set of tools
- WWW-site: <http://altarica.labri.fr>
- Yearly workshops.

## INFINITE STATE SYSTEMS

**Example:**

- Programs manipulating integers.

```
int double(int x)
{
    int y=0;
    while (x>=0){
        x=x-1;
        y=y+2;
    }
    return y;
}
```

$$(y' = 2x \wedge x \geq 0) \vee (y' = 0 \wedge x \leq 0)$$

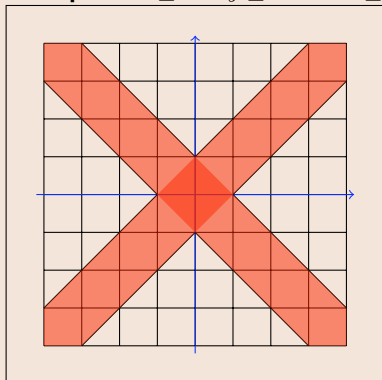
- Parametrized systems (number of clients).



## TOOLS FOR ARITHMETIC WITH ADDITION

**Goal:** MANIPULATE EFFICIENTLY SETS OF VECTOR OF INTEGERS.

**Example:**  $-1 \leq x + y \leq 1 \vee -1 \leq x - y \leq 1$



**Tools:** SATAF (2005), PRESTAF (2005), GENEPI (2006), BATOF (2006).

INTEGRATION WITH ALTARICA ([HTTP://ALTARICA.LABRI.FR](http://altarica.labri.fr))

# SUMMARY

## RESEARCH AREAS

- Computational linguistics.
- Logic Languages and Automata.
- Modelling and Verification.

## SOME DISTINCTIONS

- Gödel Prize 2002 :  
G. Sénizergues
- Citation Laureate 2004 :  
B. Courcelle

## COOPERATION

- India, Vietnam, Belgium, Poland, Germany, Israel, Portugal, Italy, Hungary, Spain, USA.
- European projects.
- National projects.
- IRISA (Rennes), LIAFA (Paris VII), LSV (Cachan), ONERA (Toulouse).