Certifying in Coq results on mobile agents: A user perspective

David ILCINKAS Joint work with Sébastien BOUCHARD

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Distributed computing

Usually

- Rather short algorithms
- Importance of <u>details</u>
- Rather long and/or tedious proofs

Specificities in distributed computing

- Local algorithm vs. global behavior
- Non-determinism
 - Asynchrony
 - Dynamicity
 - Crashes
 - Byzantines

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Detecting and preventing issues

Possible research directions to improve confidence

- Distributed certification
 - cf. Laurent Feuilloley's survey
 - self-stabilization
- Experiments
 - JBotSim from Arnaud Casteigts for example
 - Difficult to tackle non-determinism and corner cases
- Model-checking
- Certification via a proof assistant

Formal verification / model-checking

Model-checking

Automated verification based on a formalization of

- the system model
- the algorithm
- the properties to be satisfied

Pros:

- Automatic verification
- If verification fails, generally gives a counter-example
- May sometimes be able to synthesize algorithms

<u>Cons:</u>

Subject to decidability and tractability issues

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Proof assistant

- Also called Interactive theorem prover
- Checks whether a given proof of a given statement is correct
- Provides an interactive proof editor

Pros:

- More or less as powerful as paper proofs
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Cons:

- Mainly manual
- Sometimes tedious even for simple proofs

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PACTOLE project (in Coq)

- Dedicated to distributed computing by mobile robots
- Large variety of models and parameters
- Positive and negative results
- T. Balabonski, P. Courtieu, L. Rieg, S. Tixeuil, X. Urbain, ...

Our goal

Test whether **non-Coq experts a**re able to <u>certify</u> a **non-trivial** (but not-that-hard) result

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Problem: Ring exploration with stop

Model/context

- Team of robots
 - sensing the environment by taking a snapshot of it
 - that do not communicate
 - that are anonymous and oblivious
- Anonymous unoriented rings.

Goal: exploration with stop

- Each node must be visited by at least one robot.
- All robots must stop after finite time.

The Look-Compute-Move cycle

Look

The robot takes an instantaneous egocentric snapshot of the network and its robots, with strong multiplicity detection (exact number of robots at each node).

Lompute

Based on this observation, it decides to stay idle or to move to some neighboring node.

Move

In the latter case it instantaneously moves towards its destination.

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Identical oblivious semi-synchronous robots

Identical

Robots have no IDs. They execute the same program.

Oblivious

The robots have no memory of observations, computations and moves made in previous cycles.

Semi-Synchronous (asynchronous in progress)

Look/Compute/Move cycles are synchronized, but robots may sleep during some cycles.

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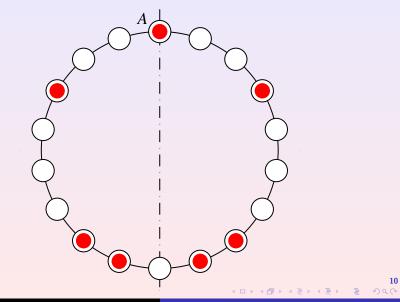
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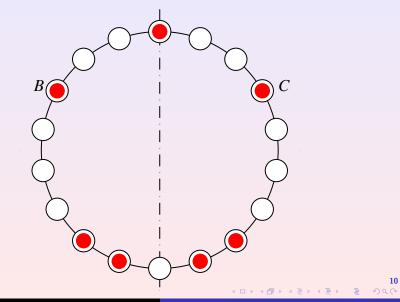
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Some precisions



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Problem definitions

Goal: exploration with stop

- Each node must be visited by at least one robot.
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Definition: Explo(*k*, *n*)

We say that exploration of an *n*-node ring is possible with k < n robots if there exists an algorithm enabling the robots to perform exploration with stop starting from any initial configuration of the k robots without multiplicity (at most one robot per node).

More formal definition: Explo(*k*, *n*), with *k* < *n* exists Algo, <u>forall</u> Adv, Config, if is_cycle(*n*,Config) <u>and</u> has_robots(*k*,Config) <u>and</u> is_flat(Config) <u>then</u> exploStop(Algo, Adv, Config)

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Already in PACTOLE

- o not Explo(1, n)
- not Explo(k, n) if k divides n

Our "new" result

for every positive integer m, not Explo $(k, n) \implies$ not Explo(k * m, n * m)

 $\mathsf{Proved via: Explo}(k \ast m, n \ast m) \Longrightarrow \mathsf{Explo}(k, n)$

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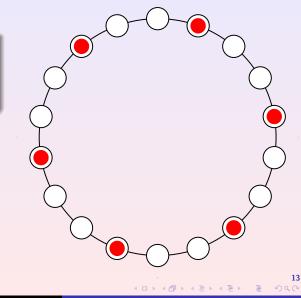
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When k divides n

Lemma

Impossible to stop (and sometimes to explore) when k|n.



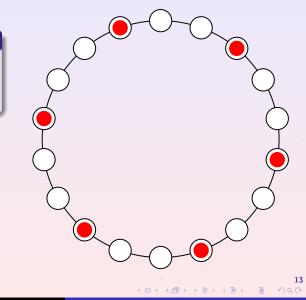
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When k divides n

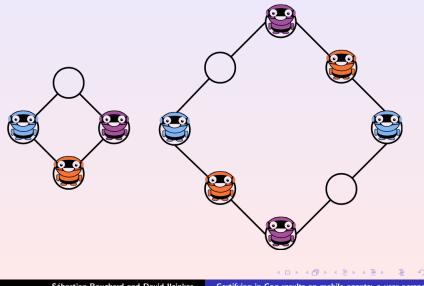
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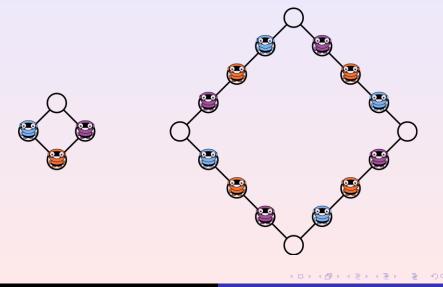
"Expanding" a "small" configuration



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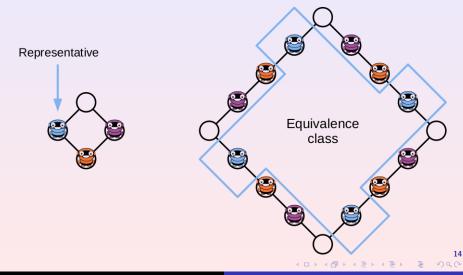
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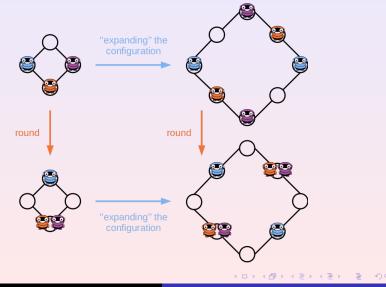
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"Similarity" of the two executions



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Sketch of proof (1/2)

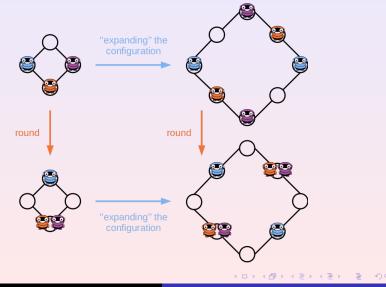
- Let \mathcal{I}_m and \mathcal{I}_1 be any "corresponding big and small instances".
- ² We assume that there exists an algorithm \mathcal{A}_m which achieves exploration with stop in \mathcal{I}_m regardless of the demon and of the initial configuration.
- Let d₁ be any demon that A₁ could face when trying to explore I₁ and let c₁ be any initial configuration for the execution of A₁.
- Let c_m be the "expansion" of c_1 .
- Let d_m be the demon which at any round, for any class c, activates all the robots of c iff d₁ activates the representative of c
- Algorithm \mathcal{A}_m achieves exploration with stop in particular when facing d_m from the initial configuration c_m .

Sketch of proof (2/2)

- We build the algorithm A_1 which gives the same instructions as A_m facing d_m from c_m but only to the robots which appear in \mathcal{I}_1 .
- Let \mathcal{E}_m be the execution of \mathcal{A}_m facing d_m from c_m .
- **9** Let \mathcal{E}_1 be the execution of \mathcal{A}_1 facing d_1 from c_1 .
- **(D)** Let \mathcal{E}'_m be the execution composed of the "expansions" of the configurations of \mathcal{E}_1 .
- **(1)** We prove that \mathcal{E}_m and \mathcal{E}'_m are "the same".
- ⁽²⁾ We deduce that A_1 achieves exploration with stop in \mathcal{I}_1 regardless of the demon and of the initial configuration.

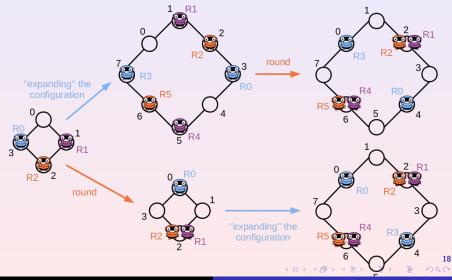
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Certifying in Coq results on mobile agents: a user perspective

• Coq basics: definitions (Gallina) and proofs (tactics)

- Onstructive logics
- Setoids (sets equipped with an equivalence relation)
- Type classes (allows to make parameters implicit)
- Induction and coinduction
- Trying to prove statements that are indeed true.
- Prove all the
 - Clearly [...]
 - It is easy to see that [...]
 - Similarly, [...]

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Some facts/numbers

Preliminary expertise

- <u>David</u>: The local Coq working group (since 2018) and the PADEC project (on self-stabilization)
- <u>Sébastien</u>: No experience with Coq (or other ITPs)

Total of 1800 lines of code

- 200 lines of definitions
- 400 lines related to Setoids (compatibility)
- 200 lines for Exploration and Stop properties
- 1000 lines for the "easy" commutativity lemma and the other "obvious" things

<u>Duration:</u> 3 months, a few hours a week

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- ... but requires some significant effort.

- Progress is continuously made to make these frameworks easier to use...
- ... and feedback would be highly appreciated by their designers.

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Quote about the Temporal Logic of Actions (TLA)

TLA does have the following disadvantages:

- It can describe only a real algorithm, not a vague, incomplete sketch of an algorithm.
- You can specify an algorithm's correctness condition in TLA only if you understand what the algorithm is supposed to do.
- TLA makes it harder to cover gaps in a proof with handwaving.

Some researchers may find these drawbacks insurmountable.

By the way, Amazon started to use formal specification and model checking in 2011, year of a major disruption in their systems...

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