

Chapter 3: `if` statements

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Comparisons and `if`

The comparison signs in Python and many other programming languages are as follows

<code>==</code>	equality
<code>!=</code>	difference
<code><</code>	less than
<code>></code>	greater than
<code><=</code>	lesser than or equal to
<code>>=</code>	greater than or equal to

Exercise 3.1

Which number is the largest 1000^{1001} or 1001^{1000} ?

Exercise 3.2

Let us consider the following code:

```
sage: a = # enter a value for a
.....: if a != 2:
.....:     print('lost')
.....: elif a == 3:
.....:     print('an instant, please')
.....: else:
.....:     print('you win')
```

What is the above program doing

- when the variable `a` is 1?
- when the variable `a` is 2?
- when the variable `a` is 3?
- when the variable `a` is 15?

Exercise 3.3

Two prime numbers p and q are said *twin* if $q = p + 2$. Find all twin prime numbers below 10000.

Exercise 3.4

Find the smallest and largest integers in the set

$$\{a^b - b^a : a \in \{1, 2, \dots, 5\}, b \in \{1, 2, \dots, 5\}\}$$

Exercise 3.5

Recall that the method `digits` of an integer returns the list of its digits:

```
sage: 1527.digits()
```

Solve [Euler problem 56](#) by finding the maximal sum of digits of numbers of the form a^b with both a and b lesser than 100

Exercise 3.6

Solve [Euler problem 4](#) about palindromes.

Exercise 3.7

Let us consider the following list of integers:

```
sage: l = [123, 414, 264, 18, 689, 21, 5571, 28, 589, 12, 111, 231,
.....: 158, 551, 250, 68, 5728, 2222, 4198, 571, 28, 518, 999, 444,
.....: 112, 689, 672, 334, 680, 273]
```

Construct two lists `leven` and `lodd` that contain respectively the even and odd elements of `l`.

Using `in` and `not in`

The condition of an `if` or `elif` statement is not necessarily a comparison. Basically, any Python object would fit!

```
sage: a = 5
sage: if a:
.....:     print('I am not zero')
```

What happens under the hood is that the object `a` (here an integer) is converted to a boolean value (`True` or `False`). You can see the boolean value of an object by using `bool`

```
sage: bool(5)
sage: bool(0)
sage: bool([])
sage: bool([0])
```

A useful construction is obtained with the keyword `in`: the result of `a in b` is whether `a` belongs to the object `b`. For example:

```
sage: 2 in ZZ
sage: 2/3 in ZZ
sage: 2/3 in QQ
sage: 1 in [3, 5, 2, 1, 2, 8]
```

```
sage: 'a' in 'Saint-Flour'
sage: 'z' in 'Saint-Flour'
```

To check that an element is not in a given object use `a not in b`:

```
sage: 10 not in Primes()
sage: 5/2 not in ZZ
```

Exercise 3.8

Using an `if` statement involving `in` inside a `for` loop, count the number of vowels in the string:

```
sage: s = 'How many vowels are present in this sentence?'
```

Count the number of consonant in the string:

```
sage: s = 'How many consonants are present in this sentence?'
```

Exercise 3.9 (Pythagorean triples)

A Pythagorean triple is a triple (a, b, c) of positive integers so that $a^2 + b^2 = c^2$. An example is $3^2 + 4^2 = 5^2$. How many Pythagorean triples are there with a, b and c smaller than 100?

Solve [Euler problem](#) by finding the unique Pythagorean triple so that $a + b + c = 1000$

Combining conditions `or`, `and` and `not`

To make even more complicated tests you can combine them. The main operators for this are `or`, `and`.

```
sage: n = 17
sage: if n.is_prime() and (n+2).is_prime():
.....:     print('a twin number!')
```

Exercise 3.10

Let us call a positive integer n a triple twin if all of $n, n+2$ and $n+6$ are primes. How many triple twins are there smaller than 10000?

The operator `not` is used for negation of a condition.

```
sage: not True
sage: not False
```

More exercises

For more exercises in the same vein you can challenge yourself with

- [Euler problem 30](#) (sum of certain numbers)
- [Euler problem 33](#) (digit cancelling fractions)
- [Euler problem 34](#) (numbers which are sum of factorials of their digits)
- [Euler problem 35](#) (circular primes)

- [Euler problem 36](#) (integers palindromic in base 2 and 10)
- [Euler problem 37](#) (truncatable primes)
- [Euler problem 38](#) (integer right triangles, aka pythagorean triples)
- [Euler problem 39](#) (binomials greater than a milion)
- [Euler problem 40](#) (continued fractions)