

IMA2017_LP_demo

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1 Mixed Integer Linear Programming demo (IMA 2017)

We show how Sage can be used to do linear optimization with different kind of real numbers:

- floating point numbers (GLPK, CBC/Coin-OR, ...) - rational (PPL) - algebraic numbers (Sage generic implementation)

1.1 Example 1

Let us consider the following problem

maximize $f(x_0, x_1, x_2) = 3x_0 + 2x_1 + x_2$ under the constraints - $x_0 \geq 0, x_1 \geq 0, x_2 \geq 0$ - $7x_0 \leq x_1 + x_2$ - $5x_1 \leq 3x_2$ - $9x_0 + 8x_1 + 7x_2 = 27$

```
In [ ]: MixedIntegerLinearProgram?  
  
In [ ]: M = MixedIntegerLinearProgram()  
  
In [ ]: x = M.new_variable(nonnegative=True)  
  
In [ ]: M.add_constraint(7*x[0] <= x[1] + x[2])  
        M.add_constraint(5*x[1] <= 3*x[2])  
        M.add_constraint(9*x[0] + 8*x[1] + 7*x[2] == 27)  
  
In [ ]: M.set_objective(3*x[0] + 2*x[1] + x[2])  
  
In [ ]: M.solve()  
  
In [ ]: M.get_values(x)  
  
In [ ]:  
  
In [ ]: M.get_backend()  
  
In [ ]:  
  
In [ ]: # to solve over rationals, just rerun the example by setting  
#  
# M = MixedIntegerLinearProgram(solver='PPL')  
#  
#####
```

```

#
# or to use CBC
# needs to install cbc first with
#
#      $ sage -i cbc
#      $ sage -b
#
# and then
#
# M = MixedIntegerLinearProgram(solver='CBC')

```

1.2 Solving over $\mathbb{Q}[\sqrt{5}]$

We consider the regular dodecahedron and maximize the linear functional $\sqrt{5}x_0 + x_1 + x_2$ on it.
(why is it not in the documentation!?)

```

In [ ]: poly = polytopes.dodecahedron()

In [ ]: poly

In [ ]: lp, x = poly.to_linear_program(solver='InteractiveLP', return_variable=True)

In [ ]: lp

In [ ]: lp.show()

In [ ]:

In [ ]: K = poly.base_ring()
K

In [ ]: sqrt5 = K.gen()

In [ ]: sqrt5**2

In [ ]: lp.set_objective(sqrt5 * x[0] + x[1] + x[2])

In [ ]: lp.solve()

In [ ]:

In [ ]: vals = lp.get_values(x)
opt = vector((vals[0], vals[1], vals[2]))
obj = vector((sqrt5, 1, 1))

In [ ]: vals

In [ ]: print opt

In [ ]: poly.plot(alpha=0.3) +
    point3d([opt], color='red', pointsize=50) +\
    arrow(opt, opt+obj/2, color='yellow')

In [ ]:

In [ ]:

```